

## MODELING TURBOCHARGER OF MARINE DIESEL GENERATOR ENGINE IN STEADY LOAD CONDITIONS

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**Abstract:** *This paper presents a model of the turbocharger for a marine diesel generator engine which used on ships. Based on the laws of thermodynamics, mean value model and Matlab/Simulink computational environment, the submodels have been built to represent for components of the turbocharger, and a complete model including the submodels and their relationships describes the turbocharger's internal performances. The diesel - turbocharger combination is simulated at some usual operation modes at different steady loads (0% - 100%) with constant speed. At each regime of load, the key characteristics are varied, for example mass flow, turbine speed, efficiency and temperature. In the practical operation, these parameters are important to evaluate engine conditions, however they are very difficult to measure. Therefore, this is meaningful in predicting turbocharger operations and maintenance activities.*

**Keywords:** Model, turbocharger, marine diesel generator engine, mass flow, efficiency.

### 1. INTRODUCTION

The turbocharger has been applied on internal combustion engine in the early 20<sup>th</sup> century, it is particularly installed on ships to increase rapidly the diesel engine power output. Nowadays turbocharging is also critical for emission control and downsizing engines.

It is obvious that turbocharging is the most useful technique to improve diesel engine efficiency and reduce emissions. Because of the complexity and high cost at laboratory, the modelling method is widely applied to research internal performance of the turbocharger and save the cost and time with affordable results.

Many researchers in universities and manufacturers have been studying and improving the turbocharger. Watson and Janota (Watson and Janota 1982) summarized the concept of turbocharging and built key individual equations for each kind of turbocharger that are the background of many researches. Lars Eriksson and Lars Niesel (Eriksson and Nielsen 2014) described models for the compressor and turbine that fit into the mean value

model framework. Turbocharger modelling is considered complex and difficult, therefore, parameterization method based on compressor and turbine flow and efficiency maps are carried out in the study of (Jung et al. 2002) and (Bozza et al. 2011). In recent years, in response to highly emission regulations many technologies, for example VGT (variable geometry turbine), EGR (exhaust gas recirculation), twin turbo, have been developed by manufacturers ABB, Honeywell, BorgWarner, etc and achieved many excellent successes.

There are many different ways of modelling, here is a model starting by conveying the principle theories, then continue with the details of submodels to make the complete model. The main target of this paper is to build a model which can clearly describe thermodynamic relationships among internal components, based on that predict their characteristics at different modes of load (0%, 25%, 50%, 75%, 100% load). The object of simulation is a diesel generator engine which used on ships. The accuracy of model can be checked with the compressor map which is provided by the supplier.

### 2. BACKGROUND

For modelling in this paper, some main concepts are background that presents as below.

Quasi-steady method: Following this method, in

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specific system aerodynamic characteristics (velocity, temperature, pressure, density) only are the function of time and one space co-coordinate.

Laws of thermodynamics: They are widely applied in science and in this paper, they are the foundation to set up the formulas.

Mean value model: The parameters and variables are considered average values in the model.

### 3. MODEL STRUCTURE

#### 3.1. Cylinder model

Pressure and temperature of gas through the cylinder: Based on the first law of thermodynamics of the gases inside the combustion chamber, equations of the fuel burning process (Miyamoto et al. 1985) and the thermo-exchange with the combustion chamber wall (Woschni 1967). The energy equation applied to the cylinder, can be rewritten as:

$$\frac{dp}{d\phi} = -k_{\gamma} \frac{p}{V} \frac{dV}{d\phi} + \frac{(k_{\gamma}-1)}{V_{cyl}} \left( \frac{\partial Q_{in}}{\partial \phi} - \frac{\partial Q_{loss}}{\partial \phi} \right) \quad (1)$$

$$\frac{dT}{d\phi} = \frac{dp}{p} \frac{1}{d\phi} + \frac{dV}{V} \frac{1}{d\phi} \quad (2)$$

Where  $p$  (N/m<sup>2</sup>),  $V$ (m<sup>3</sup>)- gas pressure and cylinder volumetric correspond to crank angle  $\phi$ ,  $\partial Q_{in}/\partial \phi$  - heat release rate while burning fuel;  $\partial Q_{loss}/\partial \phi$  - exchange heat through cylinder wall;  $k_{\gamma} = c_p/c_v$  - ratio of specific heats.

To solve system of equations (1) & (2), some key boundary conditions used (heat law of fuel burning, law of heat transfer, intake and outlet mass flow of cylinders).

#### Law of fuel burning process.

The increment heat  $\partial Q_{in}$  is calculated as:

$$\frac{\partial Q_{in}}{\partial \phi} = Q_{in} \frac{dx}{d\phi} \quad (3)$$

Where, the cumulative burn fraction of fuel ( $x$ ) is based on double Weibe's formula (Miyamoto et al. 1985)

$$\frac{dx}{d\phi} = \frac{dx_1}{d\phi} + \frac{dx_2}{d\phi} \quad (4)$$

$$\frac{dx_1}{d\phi} = \frac{Q_p}{Q_{in}} a(m_p + 1) \frac{1}{\phi_p} \left( \frac{\phi - \phi_s}{\phi_p} \right)^{-a \left( \frac{\phi - \phi_s}{\phi_p} \right)^{m_p + 1}} \quad (5)$$

$$\frac{dx_2}{d\phi} = \frac{Q_d}{Q_{in}} a(m_d + 1) \frac{1}{\phi_d} \left( \frac{\phi - \phi_s}{\phi_d} \right)^{-a \left( \frac{\phi - \phi_s}{\phi_d} \right)^{m_d + 1}} \quad (6)$$

Where  $dx/d\phi$  combustion law;  $dx_1/d\phi$  premix combustion law;  $dx_2/d\phi$  diffusion combustion law;  $a$  Weibe efficiency factor;  $m_p$  premix combustion quality factor;  $m_d$  diffusion combustion quality factor;  $\phi_s$  start of combustion;  $\phi_p$  duration of premix combustion;  $\phi_d$  duration of diffusion combustion.  $\phi_s$  is the start of ignition angle of injected fuel, which in turn is affected by the time of ignition delay  $\tau_i$  (s).

**Heat transfer law.** Newton model (Ferguson and Kirkpatrick 2015) is used to calculate the heat transfer through surface of the combustion chamber:

$$Q_{loss} = hA(T - T_w) \quad (7)$$

Where,  $h$ - heat transfer coefficient (W/m<sup>2</sup>K),  $A$  - exposed combustion chamber surface area (m<sup>2</sup>);  $T$ - temperature of the cylinder gas (°K);  $T_w$  - cylinder wall temperature (°K).

Heat transfer coefficient  $h$  is given by Woschni (Woschni 1967):

$$h = 3.26p^{0.8} U^{0.8} b^{-0.2} T^{-0.55} \quad (8)$$

Where,  $p$  - gas pressure;  $b$  - cylinder bore;  $T$  - gas temperature;  $U$  - gas velocity.

During combustion and expansion, gas velocity is given by:

$$U = 2.28 \bar{v}_p + 0.00324 \frac{V_d T_{in}}{P_{in} V_a} p \quad (9)$$

Where,  $v_p$  - mean piston velocity (m/s);  $V_d$  - displacement volume (m<sup>3</sup>);  $T_{in}$ (K),  $p_{in}$ (N/m<sup>2</sup>),  $V_a$  (m<sup>3</sup>)- gas temperature, gas pressure and cylinder volume at bottom dead center;

**Intake and outlet mass flow.** According to (Heywood 1988), the intake and outlet mass flow of cylinder calculated as

$$m_{air} = \rho_{air} \frac{P_{in}}{R_{air} T_{in}} \quad (10)$$

$$m_{out} = m_{air} + m_{fuel} \quad (11)$$

Where  $\rho_{air}$ (kg/m<sup>3</sup>) the density of the intake air,  $R_{air}$ (J/kg.K) the gas constant of intake air,  $m_{fuel}$  the mass of injected fuel (kg).

#### 3.2. Turbinemodel

The turbine is a kind of machine, in which the

exhaust gas releases the energy on the turbine blades. The model of turbine includes submodels: efficiency, exhaust mass flow, nozzle vanes, and power.

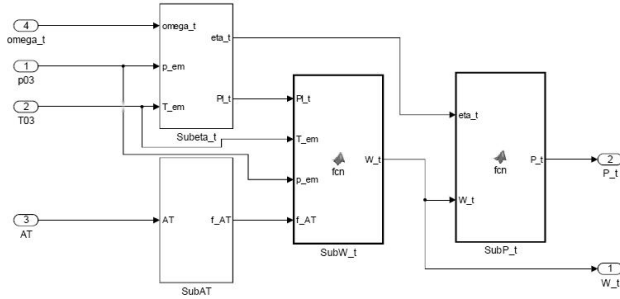


Figure 1. Turbine layout

### Turbine efficiency submodel

The turbine efficiency depends on the blade speed ratio (BSR). The BSR is defined as the ratio of the rotor tip velocity to the velocity that would be achieved by the gas following isentropic expansion from the inlet conditions to the pressure at the exit from the turbine (Watson and Janota 1982).

$$BSR = \frac{\omega_t R_t}{\sqrt{2c_{pe} T_{03} \left(1 - \pi_t^{\frac{k_e - 1}{k_e}}\right)}} \quad (12)$$

Where  $R_t$  the turbine blade radius (m),  $\omega_t$  is the turbine speed (rad/s),  $T_{03}$  the temperature at inlet turbine (K).

The efficiency turbine  $\eta_t$  varies with BSR following parabolic curves, therefore, it can be expressed by a quadric function in BSR (Eriksson and Nielsen 2014)

$$\eta_t = \eta_{t,max} \left(1 - \left(\frac{BSR - BSR_{t,max}}{BSR_{t,max}}\right)^2\right) \quad (13)$$

Where  $\eta_{t,max}$  is the maximum of efficiency at  $BSR_{t,max}$  ( $\eta_{t,max}$ ,  $BSR_{t,max}$  are tuning parameters)

### The exhaust mass flow submodel

The exhaust mass flow rate can be expressed in a function of the temperature, pressure at the inlet  $p_{03}$ , the function of pressure ratio  $f(\pi_t)$ , the function of the nozzles cross sectional area  $f(A_T)$ . It is assumed that the mass flow rate through the nozzles is the same as passing through the turbine, the equation of turbine mass flow rate presents as below

$$\dot{m}_t = A_{T,max} \frac{P_{03}}{\sqrt{R_e T_{03}}} f_{\pi_t}(\pi_t) f(A_T) \quad (14)$$

Where  $R_e$  is the gas constant;  $k_e = c_p/c_v$ ;  $A_{T,max}$  is the maximum of nozzles cross sectional area;  $f_{\pi_t}(\pi_t)$ ,  $f(A_T)$  are sub functions of  $\pi_t$ ,  $A_T$  which are calculated below.

### The nozzle submodel

The nozzles are the components of turbine, the exhaust gas must pass through it before impacting on the blade. To describe behaviour of nozzles, we use the sub model  $A_{eff}$  ( $A_{eff}$  is the cross section of nozzles),  $A_{eff} = A_{T,max} f(A_T)$ . According to (Jung et al. 2002), the equation  $f(A_T)$  can be modelled as:

$$f(A_T) = c_1 + c_2 \sqrt{1 - \left[\frac{A_T - c_3}{c_4}\right]^2} \quad (15)$$

Where  $c_1$ ,  $c_2$ ,  $c_3$ ,  $c_4$  are tuning parameters.

### 3.3. Compressor

The model of centrifugal compressor is mainly evaluated in terms of pressure  $p_{02}$ , efficiency  $\eta_c$ , turbine speed  $\omega$  and air mass flow rate  $\dot{m}_c$  (Figure 2).

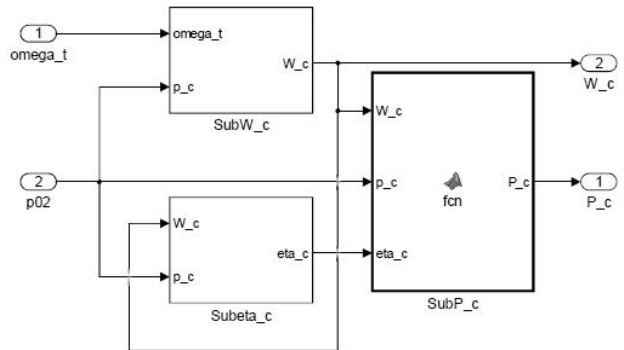


Figure 2. Compressor layout in Simulink environment

The outlet temperature of the compressor  $T_2$  is modelled as (Yin et al. 2017)

$$T_2 = \frac{1}{\eta_c} T_{amb} \left(\pi_c^{\frac{k_a - 1}{k_a}} - 1\right) \quad (16)$$

Where,  $T_{amb}$  is the ambient temperature,  $\eta_c$  is the compressor efficiency,  $k_a$  is the intake gas specific heat ratio,  $\pi_c$  is the compressor ratio.

### Compressor efficiency submodel

In the practice, compressor efficiency is modelled through the mass flow coefficient dimensionless  $\Phi$  (Eriksson and Nielsen 2014)

$$\Phi = \frac{\dot{m}_c}{n_c D^3} \frac{RT_{amb}}{P_{amb}} \quad (17)$$

Quadratic form Compressor Efficiency

$$\chi(\Phi, n_c) = \begin{bmatrix} \Phi - \Phi_{max} \\ n_c - n_{c,max} \end{bmatrix} \quad (18)$$

$$\eta_c(\chi) = \eta_{c,max} - \chi^T Q_\eta \chi$$

Where  $Q_\eta \in \mathbb{R}^{2 \times 2}$  is a symmetric and positive definite matrix.  $\Phi_{max}, n_c, n_{max}$  and the elements in  $Q$  are tuning parameters;  $T_{amb}, P_{amb}$  are the ambient temperature and pressure.

### 3.4. Turbine and Compressor balance

Figure 3 shows the pressures, temperatures, mass flow rate at the inlet and outlet of turbocharger and describes the relationships in Simulink environment.

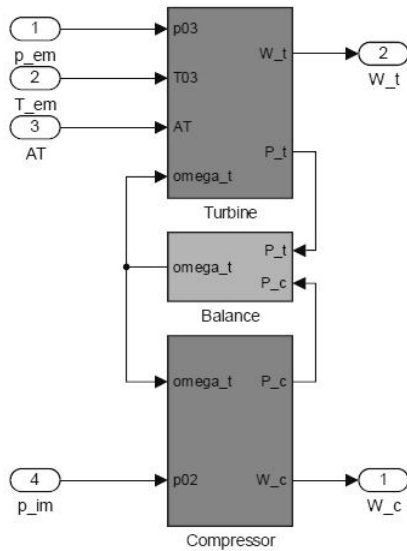


Figure 3. Turbocharger layout in Simulink environment

The laws of thermodynamics are used in this situation. The turbine and the compressor are mounted on a common shaft, the energy is transferred between two components. The balance of the turbine and the compressor is expressed as (19)

$$P_t \eta_m = P_c \quad (19)$$

Where  $P_t, P_c$  are turbine and compressor power respectively;  $\eta_m$  is the friction coefficient.

### 3.5. Engine Load (Output Power)

The engine load is the output power ( $P_b$ ), which can be calculated through indicated and friction power. Indicated Power is defined as

the power developed by combustion of fuel inside the engine cylinder

$$W_i = \int p dV \quad (20)$$

For diesel engine, indicated power is

$$P_i = i W_i n / 2 \quad (21)$$

Where  $i$  is the number of cylinders;  $n$  is the engine speed (rpm)

Output power,  $P_w$ , is the rate which work is done; therefore, it is less than the indicated power due to frictional loss.

$$P_w = P_i - P_f \quad (22)$$

Where  $P_f$  is the friction power (loss power).

## 4. RESULTS AND DISCUSSIONS

### Simulink model:

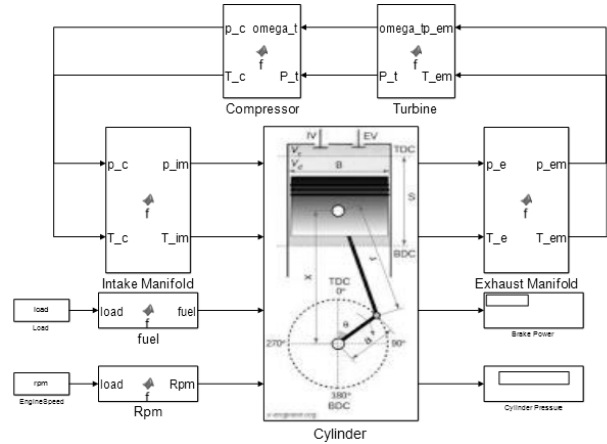


Figure 4. Simulink model of diesel and turbocharger

**Object of modelling:** The object is a marine diesel engine, Yanmar S185L, which is used on ships, assuming that engine speed is unchanged, 900 rev/min. Its turbocharger is VTR160, manufactured by ABB Group.

Table 1. Engine and turbocharger parameters

Parameters	Values
Numbers of cylinder	6
Bore x stroke (mm x mm)	185 x 230
Nominal speed (rpm)	900
Nominal power (kW)	447
Compressor diameter (mm)	170
Turbine diameter (mm)	172

#### 4.1. Speed and mass flow rate

The turbocharger speeds (rev/min) and mass flow vary according to load modes, which is shown in

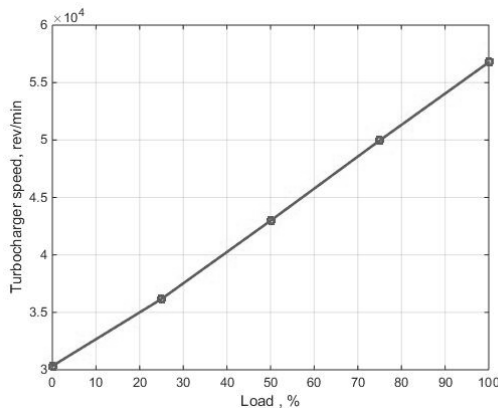


Figure 5. Turbospeed varies to loads

Figure 5 and Figure 6. The speed of turbine varies from 30.000 rev/min at idle load to 57.000 rev/min at full load.

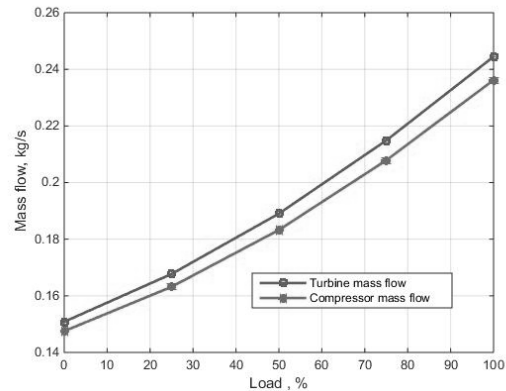


Figure 6. Mass flow rates diagram

#### 4.2. Efficiency and temperature

The efficiencies and temperatures of turbine and compressor are shown in Figure 7 and Figure 7. At the low load conditions, the compressor efficiency is very low, it increases when the load increases. The

turbine efficiency is not changed much at every load. The range of turbine's inlet temperature is (620 ÷ 830<sup>0</sup>K), the compressor's outlet temperature is not changed much (300 ÷ 345<sup>0</sup>K)

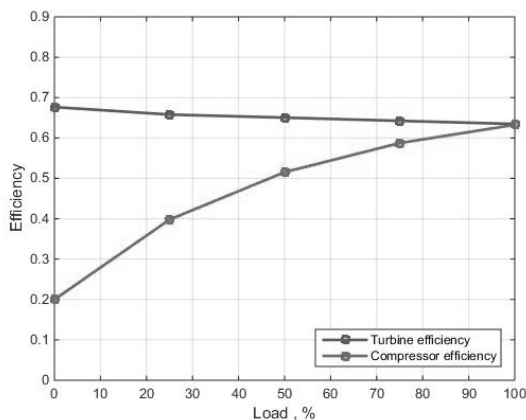


Figure 7. Turbocharger efficiency

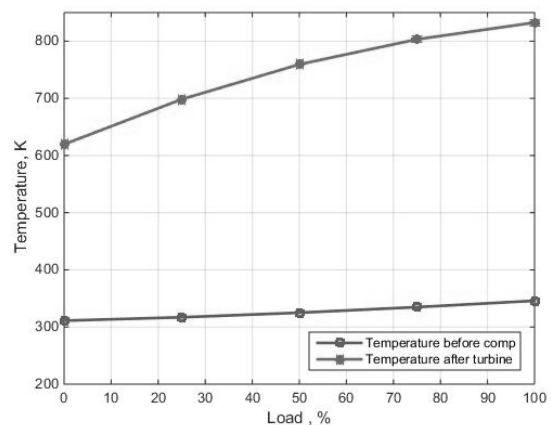


Figure 8. Inlet and outlet temperature

### 5. CONCLUSION

The paper has achieved some results:

Summarize the key thermodynamic characteristics of a diesel engine and its turbocharger.

Build a model in Matlab/simulink environment, which combines the diesel and the turbocharger. The relationship between them is very complex, at this situation we considered their working at the steady load modes. The model has described the contact

between internal characteristics and simulated their thermodynamic processes.

The results are presented and discussed enlightening the key parameters for the turbocharger operation at different of steady loads, for example (speed, efficiency, mass flow, temperature). In the practical, these parameters are very difficult to measure, therefore it is meaningful to save time and cost in maintenance activities and operations.

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### Tóm tắt:

## MÔ HÌNH CỤM TĂNG ÁP TUA BIN KHÍ CỦA ĐỘNG CƠ DIESEL TÀU THỦY LAI MÁY PHÁT ĐIỆN TRONG CÁC ĐIỀU KIỆN TẢI ỔN ĐỊNH

Bài báo trình bày một mô hình cụm tua bin tăng áp của động cơ diesel tàu thủy lai máy phát điện. Dựa trên các định luật nhiệt động, mô hình giá trị trung bình và môi trường tính toán Matlab/Simulink, các mô hình con được thiết lập đặc trưng cho các bộ phận của bộ tăng áp. Sau đó một mô hình hoàn chỉnh bao gồm các mô hình con và mối liên hệ giữa chúng được xây dựng để mô tả các đặc tính bên trong bộ tăng áp. Tổ hợp diesel – turbocharger được mô phỏng tại các chế độ hoạt động thông thường với các điều kiện tải khác nhau (0% - 100%) và tốc độ không thay đổi. Với mỗi chế độ của tải, các đặc trưng cơ bản thay đổi theo, ví dụ như lưu lượng, tốc độ tua bin, hiệu suất và nhiệt độ. Trong thực tế khai thác, những thông số này rất quan trọng để đánh giá tình trạng động cơ, tuy nhiên lại rất khó đo kiểm được. Vì vậy, điều này rất có ý nghĩa trong dự đoán hoạt động tăng áp và quá trình bảo dưỡng nó.

**Keywords:** Mô hình, tăng áp, động cơ diesel lai máy phát điện, lưu lượng, hiệu suất.

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